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*This promotional copy includes answers for Chapter 1 only. The final text will include answers for all chapters in the text.